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HARMONIC ANALYSIS AND EVALUATION OF 52 BUS IN NIGERIA TRANSMISSION NETWORK

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Abstract: The 330kV grid in Nigeria, consisting of 52 buses, is confronted with significant challenges, including voltage instability, extended transmission lines, inherent transmission line characteristics, and substantial power losses, which adversely impact both power generation and distribution systems. This study focuses on the harmonic analysis of the Nigerian 52-bus grid, comprising 52 buses, 18 generating stations, and 65 transmission lines. Utilizing ETAP 16.0 as the analytical tool, the research investigates harmonic orders on the 330kV line network in Nigeria. Simulations were conducted using the ETAP 16.0 software package, with input parameters encompassing relative amplitudes and phase angles for both current and voltage source models. Data for the study were sourced from the Transmission Company of Nigeria (TCN). The obtained results reveal that some bus voltages exceed the prescribed standard limits. Consequently, it can be deduced from the findings that the existing Nigerian 52-bus grid grapples with considerable line losses, necessitating compensation through the implementation of reactive power support mechanisms, such as Flexible Alternating Current Transmission Systems (FACTS) devices, to optimize line utilization effectively.

Keywords: Load flow, Harmonic Order, Transmission Line, Voltage instability, Power Quality.

1 Introduction

The Electrical Power sector plays an important role in the socioeconomic development of a nation. However, in the case of Nigeria, the power network is facing multifaceted challenges that demand intervention. The power system is overloaded, supplying beyond nominal capacity. With a growing population, the demand for electrical energy has surged exponentially, outpacing the capacity of the existing infrastructure. Generation stations situated far from load centres transmit their electrical energy via long, radial and not up-to-standard transmission lines [1]. This noticeable demand-supply gap has resulted in a strain on the power system, giving rise to voltage fluctuations, equipment overheating and diminished power quality, ultimately compromising the overall reliability of the grid [2]. However, the urgency for a comprehensive system analysis of the electrical network in Nigeria cannot be overstated as she's at

an all-time peak of industrial production and thus ensuring a stable power supply is crucial to sustain this growth.

Incorporated in the existing 330kV Nigeria grid network are complex equipment such as transmission lines, transformer tappings, various alternators, reactors, compensators, phase shifters, synchronous condensers, static capacitors, etc, and Power quality meters which serve as the medium for data collection. With the availability of the data comes the avenue for system status and operation assessment, analysis by network designers, and network system forecast [3]. This work used the harmonic analysis method of analysing power systems to evaluate the improved 52-bus Nigeria 330kV power network.

The harmonic analysis offers a granular perspective on the power system in the frequency domain as opposed to the time domain, pinpointing sources of distortion and hence enabling the development of mitigation strategies that enhance power

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quality [4]. Using Electrical transient and analysis program (ETAP), one of the best tools to study harmonics in the power system, this work navigated the complexities of the 52-Bus Nigeria Transmission Network evaluating the network performance, effectiveness and alternative plans for network reconfiguration. The level of harmonic distortion in the system is indicated by the Total Harmonic Distortion (THD) index, which is used to measure current and voltage dimensions.

THD is defined as the root mean square (rms) value of the hth harmonic component divided by the respective rms value of the fundamental component, multiplied by 100% [5]. The THD of current can vary from 5% to 100%, while THDs of voltage less than 5% are generally considered acceptable. Values exceeding 5% may indicate problematic equipment, devices, or arrangements [6].

Harmonic modelling in power networks is a crucial aspect of electrical engineering that involves the analysis and understanding of harmonic distortions within an electrical system. These harmonic distortions emerge from the operation of various equipment and inductive and capacitive loads in the system causing problems such as voltage distortion, overheating and power quality issues. To address these problems, we use harmonic modelling to identify possible sources of harmonics in a particular system. Key steps needed to conduct a harmonics study come from research experience and practical insights. However, these steps encompass the acquisition of a single-line diagram of the network, pinpointing the point of common coupling, identifying harmonic sources, conducting harmonic measurements, and modelling network components using simulation software like ETAP. After, there is a comparison of the results with national standards.

In order to create a reliable harmonic model for any network, it is imperative to accurately represent all the network components. To conduct comprehensive harmonic modelling and simulation of a given system, two critical considerations have been identified and reviewed to bridge the gap and yield more dependable results. ETAP is employed, and on-site measurements of harmonic currents are used to fine-tune computer-based harmonic current models to match and validate the measured data. The Power System Computer Aided Design/Electromagnetic Transients including DC (PSCAD/EMTDC) software is utilized to build simulation models based on laboratory-measured waveforms. A generalised model for distribution systems has been successfully implemented for practical case studies, using verified simulation models for a range of industrial and household electrical equipment and appliances. Similarly, DigSilent/PowerFactory serves as the simulation software used to assess future levels of harmonic distortion in the power grid, based on the present harmonic current source model developed from measured data [7].

2. Methodology

$$F(t) = periodic f unction of Fourier Series f(t)$$

$$= C_{0} + \sum_{h=1}^{\infty} C_{h} \cos(h\omega t + \theta_{h})$$

$$C_{o} = \frac{1}{T} \int_{o}^{T} f(t) dt, C_{h} = \sqrt{A_{h}^{2} + B_{h}^{2}}$$

$$A_{h} = \frac{2}{T} \int_{o}^{T} f(t) \cos(h\omega t) dt$$

$$B_{h} = \frac{2}{T} \int_{o}^{T} f(t) \sin(h\omega t) dt$$
(3)

(4)

(5)

where:

h: order of the harmonic

 $C_{o: \text{ coefficient of the nth harmonic}}$

 $\dot{\omega}$: natural frequency

 A_h , B_h : sine and cosine coefficients of the nth harmonic

Total Harmonic Distortion(THD) in Voltage(Percent):

$$THD_{v}\% = \frac{\sqrt{\sum_{h=2}^{\infty} V_{h}^{2}}}{V_{i}} \times 100$$

Total Harmonic Distortion(THD) in Current(Percent):

$$THD_{i}\% = \frac{\sqrt{\sum_{h=2}^{\infty} I_{h}^{2}}}{I_{i}} \times 100_{(6)}$$

where:

 $V_{h},\,I_{h}:\,h^{th}\,Harmonic \mbox{ component of the voltage and current,}$

V_i , I_i : fundamental component

$$\widetilde{V}_{H} = \sqrt{\sum_{h=2} \widetilde{V}_{h}^{2}}$$
(7)

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$$\widetilde{I}_{H} = \sqrt{\sum_{h=2} \widetilde{I}_{h}^{2}}$$

$$\widetilde{I} = \sqrt{\sum_{h=1}^{\infty} \widetilde{I}_h^2}$$
(9)

$$\widetilde{V} = \sqrt{\sum_{h=1}^{\infty} \widetilde{V}_h^2}$$

$$THD_{o}\% = HF \times \frac{Drive \ kVA}{SC \ kVA} \times 100$$
(11)

$$HF = \sqrt{\sum_{h=5}^{\infty} \frac{h^2 I^2}{I_i}}, \text{ Harmonic Factor}$$
(12)

$$P = \widetilde{V}\widetilde{I}_{i,1}\cos\phi_1\tag{13}$$

$$Q = \widetilde{V}\widetilde{I}_{i,1}\sin\phi_{1,S} = \widetilde{V}\widetilde{I}$$
(14, 15)

$$VA = \sqrt{S^2 - P^2 - Q^2}$$
(16)

D = Distortion

$$D^{2} = S^{2} - \left(\tilde{V}^{2}\tilde{I}_{i,1}^{2}\right) = \tilde{V}^{2}\sum_{h=2}^{\infty}\tilde{I}_{i,h}^{2}$$

$$\lambda = True \ Power \ Factor = \frac{P}{S} = \left(\frac{I_{i,1}}{I}\right)\cos\phi_{1}$$

$$= Distortion \ Factor \times Displacement \ Factor$$

Nonsine wave voltage and current

$$P = \sum_{h=1}^{\infty} \tilde{V}_h \tilde{I}_h \cos\phi_h, \quad Q = \sum_{h=1}^{\infty} \tilde{V}_h \tilde{I}_h \sin\phi_h$$
(18)

D = Distortion Power $=\sum_{n\,m}^{\infty}S_{nm}S_{nm}^* - \sum_{n\,m}^{\infty}S_nS_m^*$ (19) $S^2 = P^2 + Q^2 + D^2$ (20) $S = \sqrt{\sum_{h=1}^{\infty} \tilde{V}_{h}^{2} \tilde{I}_{h}^{2}} = \left(\tilde{V}_{1} \tilde{I}_{1}\right)^{2} + \left(\tilde{V}_{1} \tilde{I}_{H}\right)^{2} + \left(\tilde{V}_{H} \tilde{I}_{1}\right)^{2} + \left(\tilde{V}_{H} \tilde{I}_{H}\right)^{2} = S_{1}^{2} + S_{N}^{2}$ (21) $S_1 = Fundamental Apparent Power = \tilde{V}_1 \tilde{I}_1$ $S_N = Non f undamental Apparent Power$ $S_N^2 = \left(\tilde{V_1} \tilde{I}_H \right)^2 + \left(\tilde{V_H} \tilde{I}_1 \right)^2 + \left(\tilde{V_H} \tilde{I}_H \right)^2$ $\tilde{V}_{1}\tilde{I}_{H}$ = Current Distortion Power $\tilde{V}_{H}\tilde{I}_{1}$ = Voltage Distortion Power $\tilde{V}_{H}\tilde{I}_{H}$ =Harmonic Apparent Power $S_{H}^{2} = P_{H}^{2} + N_{H}^{2}$ = Total Harmonic Active Power + Total Harmonic Non Active Power (23)

$$X_{c} = Reactance \ of \ the \ capacitor = \frac{\left(V_{L-L}\right)^{2}}{\frac{VAR_{3-phase}}{(24)}}$$

METHODOLOGY FOR COMPUTING DISTORTION

$$I_{b} = Base \ current \ in \ Amps = \frac{MVA_{b} \times 10^{3}}{\sqrt{3}kV_{b}} Amps$$
(25),

$$Z_{s}(System impedance) = \frac{MVA_{b}}{MVA_{sc}} p.u.$$
(26)

(8)

(10)

 $V_{H}(Percent individual harmonic voltage distribution) = \frac{I_{h}}{I_{b}}(h) (Z_{s}$ (27)

$$THD_{v}\% = \frac{\sqrt{\sum_{h=2}^{\infty} V_{h}^{2}}}{V_{i}} \times 100$$

$$THD_i\% = \frac{\sqrt{\sum_{h=2}^{\infty} I_h^2}}{I_i} \times 100$$

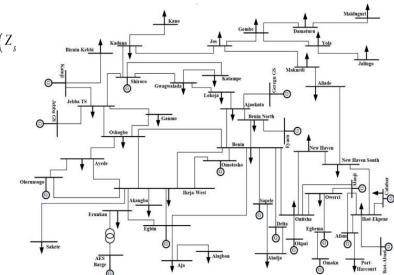


Fig 1: Single Line Diagram of Nigeria 330 kV Power Grid

h = harmonic order, $I_{H}(Percent individual harmonic distortion) = \frac{I_{h}}{I_{L}} \times 100$

(28)

(29)

Table 1

 $I_{sc} = Short Circuit current at the point under considered for the 52-bus 330 kV Nigeria Power Grid$ $I_L = Estimated maximum demand load current <math>S/N$ Line Name L(km)

Short circuit Ratio =
$$\frac{I_{sc}}{I_L} = \frac{MVA_{sc}}{MVA_D}$$
(30)

$$K Factor = \sum_{h=1}^{\infty} (h)^{2} \times \left(\frac{I_{h}}{I_{L}}\right)^{2}$$
(31)

Data Collection

The data used for this study were obtained from Transmission Company of Nigeria (TCN) and are presented in Table 1, Table 2 and Table 3. The ETAP 16.0 electrical software was used in conducting the simulation.

| S/N | Line | Name | L(km) |
|-----|-------|------------------------|-------|
| 1 | 01-02 | Egbin-Benin | 218 |
| 2 | 01-03 | Egbin-Ikeja- West | 62 |
| 3 | 01-31 | Egbin-Aja | 14 |
| 4 | 01-51 | Egbin-Erunkan | 30 |
| 5 | 02-03 | Benin-Ikeja West | 280 |
| 6 | 02-08 | Benin-Omotoso | 51 |
| 7 | 02-09 | Benin-Osogbo | 251 |
| 8 | 02-22 | Benin-Ajaokuta | 195 |
| 9 | 02-24 | Benin-Onitsha | 137 |
| 10 | 02-27 | Benin-Sapele | 50 |
| 11 | 02-28 | Benin-Delta | 41 |
| 12 | 02-48 | Benin-Benin North | 20 |
| 13 | 03-04 | Ikeja West- Akangba | 17 |

| 14 | 03-05 | Ikeja West- Sakete | 70 |
|----|-------|--------------------------|-----|
| 15 | 03-06 | Ikeja West- Ayede | 137 |
| 16 | 03-07 | Ikeja West- Papalanto | 30 |
| 17 | 03-08 | Ikeja West- Omotoso | 200 |
| 18 | 03-09 | Ikeja West- Osogbo | 250 |
| 19 | 03-51 | Ikeja West- ErunKan | 32 |
| 20 | 06-07 | Ayede- Papalanto | 60 |
| 21 | 06-09 | Ayede-Osogbo | 115 |
| 22 | 09-10 | Osogbo-Ganmo | 75 |
| 23 | 09-12 | Osogbo-Jebba TS | 157 |
| 24 | 10-12 | Ganmo-Jebba TS | 80 |
| 25 | 11-12 | Shiroro-Jebba TS | 244 |
| 26 | 11-17 | Shiroro-Kaduna | 96 |
| 27 | 11-21 | Shiroro- Katampe | 144 |
| 28 | 11-50 | Shiroro- Gwagwalada | 114 |
| 29 | 12-13 | Jebba GS-Jebba TS | 8 |
| 30 | 12-15 | Kainji-Jebba TS | 81 |
| 31 | 14-15 | Birnin Kebbi- Kainji | 310 |
| 32 | 16-17 | Kaduna-Kano | 230 |
| 33 | 17-18 | Kaduna-Jos | 196 |
| 34 | 18-19 | Jos-Gombe | 264 |
| 35 | 18-36 | Makurdi-Jos | 230 |
| 36 | 19-20 | Gombe-Yola | 240 |
| 36 | 19-20 | Gombe-Yola | 240 |

| 37 | 19-33 | Gombe- Damaturu | 135 |
|----|-------|------------------------------------|-----|
| 38 | 20-35 | Yola-Jalingo | 132 |
| 39 | 21-50 | Gwagwalada- Katampe | 30 |
| 40 | 22-23 | Ajaokuta- Geregu | 1 |
| 41 | 22-48 | Benin North- Ajaokuta | 195 |
| 42 | 22-49 | Ajaokuta- Lokoja | 38 |
| 43 | 24-25 | Alaoji-Onitsha | 138 |
| 44 | 24-26 | New Haven- Onitsha | 96 |
| 45 | 24-29 | Onitsha-Okpai | 60 |
| 46 | 24-38 | Owerri-Onitsha | 137 |
| 47 | 25-30 | Alaoji-Afam | 25 |
| 48 | 25-38 | Owerri-Alaoji | 60 |
| 49 | 25-40 | Alaoji | 38 |
| 50 | 26-39 | New Haven- New Haven South | 5 |
| 51 | 27-32 | Sapele-Aladja | 63 |
| 52 | 28-32 | Delta-Aladja | 32 |
| 53 | 30-40 | Afam-Ikot Ekpene | 90 |
| 54 | 30-41 | Afam-Port Harcourt | 45 |
| 55 | 31-52 | Aja-Alagbon | 26 |
| 56 | 33-34 | Damaturu- Maiduguri | 140 |
| 57 | 36-46 | Aliade-Makurdi | 50 |
| 58 | 38-45 | Owerri-Egbema | 30 |
| 59 | 39-40 | Ikot Ekpene- New Haven South | 153 |
| 60 | 39-46 | New Haven South-Aliade | 150 |

| 61 | 40-42 | Ikot Ekpene- Calabar | 72 |
|----|-------|----------------------------|-----|
| 62 | 40-43 | Ikot Abasi- Ikot Ekpene | 75 |
| 63 | 44-45 | Omoku-Egbema | 30 |
| 64 | 47-48 | Eyaen-Benin North | 5 |
| 65 | 49-50 | Lokoja- Gwagwalada | 140 |

| Lo ad 16 | 15 7 | 76 | Lo ad 33 | 60 | 40 | Lo ad 51 | 14 | 6 |
|----------------|---------|----|----------------|----|----|----------------|----|---|
| Lo ad 17 | 17 3 | 84 | Lo ad 34 | 50 | 30 | Lo ad 52 | 17 | 8 |
| Lo ad 18 | 89 | 43 | Lo ad 35 | 45 | 25 | | | |

Table 2

Load data of the 52-bus 330 kV Nigeria Power Grid

| Lo ad | M W | MV AR | Lo ad | M W | MV AR | Lo ad | M W | MV AR |
|----------------|---------|----------|----------------|---------|----------|----------------|--------|----------|
| Lo ad 02 | 18 8 | 91 | Lo ad 19 | 11 3 | 55 | Lo ad 36 | 60 | 30 |
| Lo ad 03 | 32 1 | 155 | Lo ad 20 | 71 | 34 | Lo ad 38 | 12 | 6 |
| Lo ad 04 | 29 7 | 144 | Lo ad 21 | 18 9 | 62 | Lo ad 39 | 60 | 30 |
| Lo ad 05 | 91 | 44 | Lo ad 22 | 60 | 29 | Lo ad 40 | 15 | 7 |
| Lo ad 06 | 17 0 | 82 | Lo ad 24 | 10 2 | 48 | Lo ad 41 | 10 | 6 |
| Lo ad 09 | 14 8 | 72 | Lo ad 25 | 16 7 | 78 | Lo ad 46 | 50 | 20 |
| Lo ad 10 | 17 0 | 82 | Lo ad 26 | 14 0 | 64 | Lo ad 48 | 18 | 8 |
| Lo ad 12 | 26 0 | 125 | Lo ad 31 | 13 9 | 65 | Lo ad 49 | 16 | 7 |
| Lo ad 14 | 71 | 34 | Lo ad 32 | 10 5 | 51 | Lo ad 50 | 10 | 4 |

Table 3

Generator data of the 52-bus 330kV Nigeria Power Grid

| Generators | Plant type | Active Power Limit (MW) |
|-----------------------|------------------|----------------------------|
| Gen 01_Egbin | Steam and Gas | 1320 |
| Gen 07_Papalanto | Gas | 335 |
| Gen 08_Omotosho | Gase | 335 |
| Gen 11_Shiroro | Hydro | 600 |
| Gen 13_Jebba | Hydro | 607 |
| Gen 15_Kainji | Hydro | 760 |
| Gen 23_Geregu | Gas | 444 |
| Gen 25_Alaoji | Gas | 480.25 |
| Gen 27_Sapele | Gas | 1080 |
| Gen 28_Delta | Gas | 960 |
| Gen 29_Okpai | Gas | 450 |
| Gen 30_Afam | Gas | 727 |
| Gen 37_AES Barge | Gas | 280 |
| Gen 42_Calabar | Gas | 562 |
| Gen 43_Ikot- Abasi | Gas | 196 |
| Gen 44_Omoku | Gas | 150 |

| Gen 45_Egbema | Gas | 340 |
|---------------|-----|-----|
| Gen 47_Eyaen | Gas | 452 |

3. Results and Discussion

The simulation results obtained are presented in Table 5 below. Table 5 presents the result of alert of the harmonic load flow obtained from Etap.

| | Study Case: HA Configuration: Normal | | n: Base e: 15-06-2022 | Fib | er Zone | |
|-------------|---|---------------|--------------------------|-----------|-------------|---------|
| | | | Offical | | | |
| Device ID | Туре | Condition | Rating /Limit | Operating | % Operating | Hamonic |
| AFAM GS | Bus IHD | Exceeds Limit | 2 | 3.45 | 172.64 | 5.00 |
| AFAM GS | Bus IHD | Exceeds Limit | 2 | 2.41 | 120.68 | 7.00 |
| AFAM GS | Bus IHD | Exceeds Limit | 1.5 | 1.54 | 102.35 | 11.00 |
| AFAM GS | Bus IHD | Exceeds Limit | 0.5 | 0.51 | 101.99 | 41.00 |
| AFAM GS | Bus IHD | Exceeds Limit | 0.47 | 0.51 | 106.94 | 43.00 |
| AFAM GS | Bus THD | Exceeds Limit | 3 | 4.9 | 163.49 | Total |
| ALAOJI GS | Bus IHD | Exceeds Limit | 1 | 2.96 | 296.49 | 5.00 |
| ALAOJI GS | Bus IHD | Exceeds Limit | 1 | 1.94 | 193.59 | 7.00 |
| ALAOJI GS | Bus IHD | Exceeds Limit | 1 | 1.84 | 183.81 | 11,00 |
| ALAOJI GS | Bus IHD | Exceeds Limit | 1 | 1.63 | 163.2 | 13.00 |
| ALAOJI GS | Bus THD | Exceeds Limit | 1.5 | 4.38 | 291.91 | Total |
| ALAOJI TS | Bus IHD | Exceeds Limit | 1 | 3.04 | 304.12 | 5.00 |
| ALAOJI TS | Bus IHD | Exceeds Limit | 1 | 1.98 | 198.46 | 7.00 |
| ALAOJI TS | Bus IHD | Exceeds Limit | 1 | 1.88 | 188.2 | 11.00 |
| ALAOJI TS | Bus IHD | Exceeds Limit | 1 | 1.67 | 166.97 | 13.00 |
| ALAOJI TS | Bus THD | Exceeds Limit | 1.5 | 4,49 | 299.16 | Total |
| ASABA | Bus THD | Exceeds Limit | 3 | 3.02 | 100.78 | Total |
| BENIN | Bus IHD | Exceeds Limit | 1 | 1.13 | 113.12 | 7.00 |
| IKOT EKPENE | Bus IHD | Exceeds Limit | 1 | 2.33 | 233.13 | 5.00 |
| IKOT EKPENE | Bus IHD | Exceeds Limit | 1 | 1.24 | 123.6 | 7.00 |
| IKOT EKPENE | Bus THD | Exceeds Limit | 1.5 | 2.76 | 183.98 | Total |
| MAKURDI | Bus IHD | Exceeds Limit | 2 | 2.09 | 104.56 | 5.00 |
| MAKURDI | Bus IHD | Exceeds Limit | 2 | 2.58 | 128.84 | 7.00 |
| MAKURDI | Bus THD | Exceeds Limit | 3 | 3.44 | 114.64 | Total |
| N,HAVEN | Bus IHD | Exceeds Limit | 2 | 2.15 | 108.1 | 5.00 |
| ONITSHA | Bus IHD | Exceeds Limit | 1 | 2.12 | 211.63 | 5.00 |
| ONITSHA | Bus IHD | Exceeds Limit | 1 | 1.66 | 165.7B | 7.00 |
| ONITSHA | Bus IHD | Exceeds Limit | 1 | 1.36 | 136.3 | 11.00 |
| ONITSHA | Bus THD | Exceeds Limit | 1.5 | 3.08 | 205.27 | Total |
| UGWUAJI | Bus IHD | Exceeds Limit | 2 | 2.19 | 109.72 | 5.00 |

| Figure 2: Alert Values of the Harmonic Load Flow |
|--|
| Simulation of Nigeria 52-bus 330kV Grid |

Conclusion

In this paper, the harmonic modelling and simulation for the Nigerian 52-bus 330kV grid network was done using the ETAP 16.0 electrical simulation software. The findings indicate that the 330kV grid network in Nigeria is plagued by several issues, including voltage instability (manifested as voltage profile violations), challenges associated with lengthy transmission lines, the inherent characteristics of these transmission lines, and subpar power quality. This is particularly pronounced in the Northern regions of the examined network. To address these issues effectively, it is recommended to incorporate more substations and additional transmission lines into the existing 330kV grid. Introducing these enhancements will create additional loops within the network, significantly improving its overall profile and performance.

References

- Akwukwaegbu, I.O., Nosiri, O.C. and Ezugwu, E.O.. Voltage stability investigation of the Nigeria 330kV interconnected grid system using eigenvalues method. American Journal of Engineering Research, 6(4), pp.168-182. 2017.
- [2] Cowart, R.H. Efficient reliability. The Critical Role of Demand-Side Resources in Power Systems and Markets, Montpelier. 2001.
- [3] Eseosa, O. and Ogujor, E.A. Determination of bus voltages, power losses and flows in the Nigeria 330kV integrated power system. International Journal of Advances in Engineering & Technology, 4(1), p.94. 2012.
- [4] Xu, W., Huang, Z., Xie, X. and Li, C. Synchronized waveforms– a frontier of databased power system and apparatus monitoring, protection, and control. IEEE Transactions on Power Delivery, 37(1), pp.3-17. 2021.
- [5] S. L. Braide Evaluation and Analysis of Harmonic Distortionon 330kV Network Case Study Selected Sub-Region Nigerian Power System for Improve Power Quality
- [6] Kassakian, J.G., Perreault, D.J., Verghese, G.C. and Schlecht, M.F. Principles of power electronics. Cambridge University Press. 2023.
- [7] T. Belgin and T. C. Kaypmaz. Harmonic Measurements and Power factor Correction in a Cement Factory, International Conference on Electrical and Electronics Engineering, Istanbul, ELECO. 1999.
- [8] Eke, A., Archibong, E., Akisot, E. and Akpama, E.J., Harmonic Analysis and Evaluation on Nigeria 330kv Lines Network For Effective Energy Planning and Delivery. 2021.